

Short pathlength corrections to energy loss in a quark gluon plasma

Based on arXiv:2305.13182

Coleridge Faraday

Supervised by A/Prof. W. A. Horowitz

SAIP Conference: 5th of July, 2023

MSc candidate, University of Cape Town

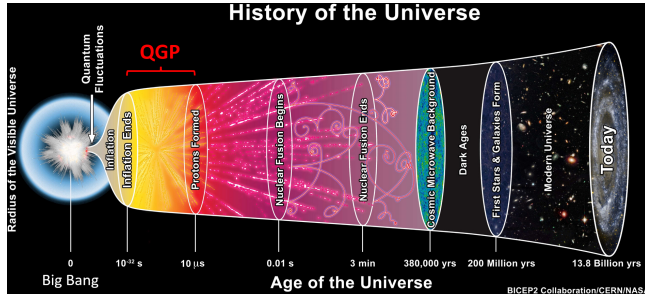


**National
Research
Foundation**



Role of QCD in understanding the universe

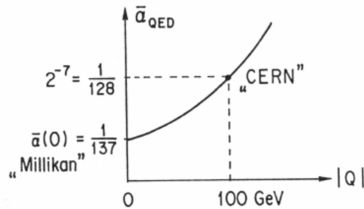
- First microseconds after the Big Bang?
- *Quark gluon plasma*: physics of a trillion degrees?
- Neutrons stars?



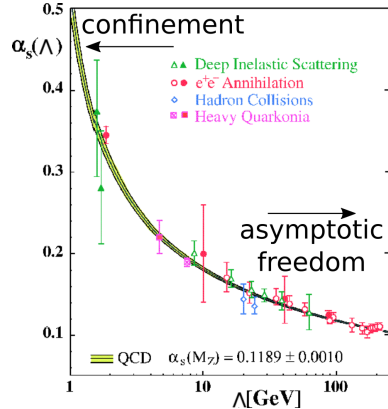
- *Quantum Chromodynamics* (QCD) describes quarks and gluons, which make up protons and neutrons

What makes QCD special?

- Coupling $\sim$ interaction strength
- Running coupling and perturbation theory
- Nonabelian gauge group



QED running coupling, perturbative at all scales of interest



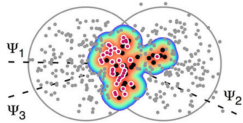
QCD running coupling, perturbative **only** at high energies

How to study QCD?

- Want to study *Quark Gluon Plasma* → high-energy heavy-ion collisions

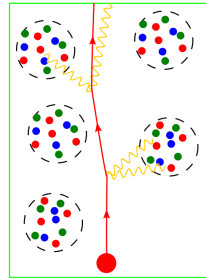
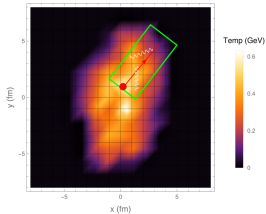
How to study QCD?

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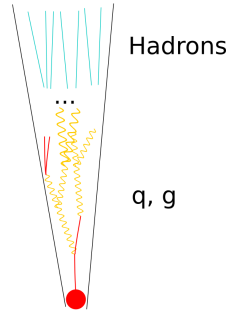
Collision sets
up geometry

QGP evolves
with hydro



Energy loss

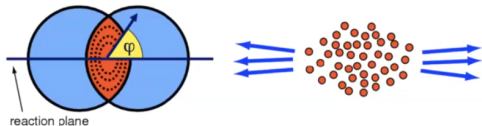
Hadronisation
and jet detection



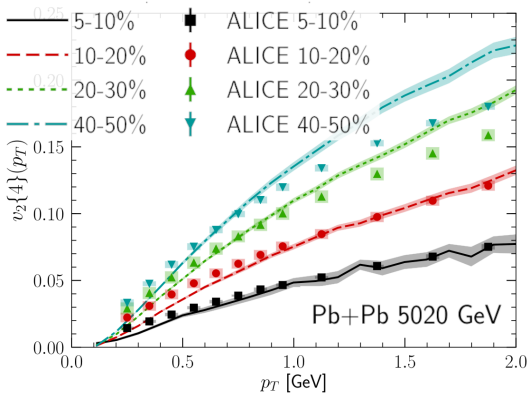
Evidence for QGP formation: Angular correlations

$$v_n \equiv \langle \cos [n (\phi - \Psi_n)] \rangle$$

- For peripheral collisions dominant v_2 due to *elliptic geometry*
- Well described by *hydrodynamic* models at low- p_T

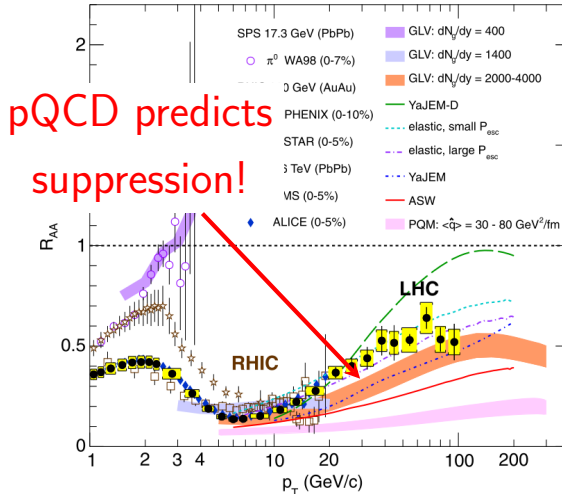


Spatial anisotropy $\rightarrow$ momentum anisotropy
(Source: CTMP talk by François Arleo)



2nd Fourier coefficient related to
azimuthal anisotropy (sig. of “*Elliptic flow*”)
(Schenke et al. 2020.14682)

Evidence for QGP formation: Energy loss

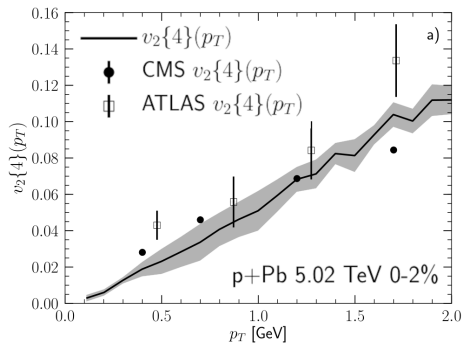


$$R_{AB}^h \equiv \frac{d\sigma_{AB}^h}{N_{\text{coll}} d\sigma_{pp}^h}$$

- N_{coll} from Glauber model, treating nucleons as independent
- Normalised s.t.
 - $R_{AB} < 1 \implies$ suppression
 - $R_{AB} = 1 \implies$ no final state effects
 - $R_{AB} > 1 \implies$ enhancement

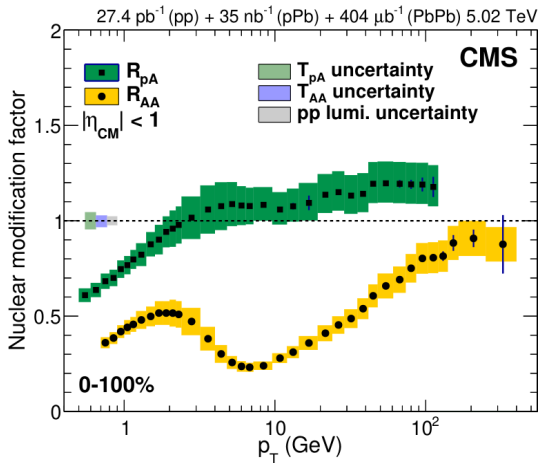
**Solid evidence for QGP in $A + A$;
 $p + A$ as a null control?**

QGP formation in small systems?

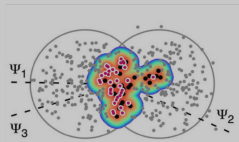


Elliptic flow in p+A?
(Schenke et al. 2020, 2005.14682)

+ other signs (quarkonium suppression, strangeness enhancement)

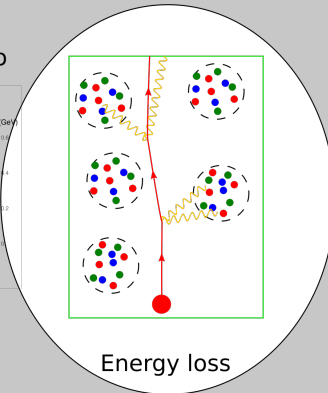
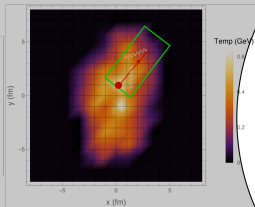


Final state enhancement in p+A?
(CMS 2017, 1611.01664)

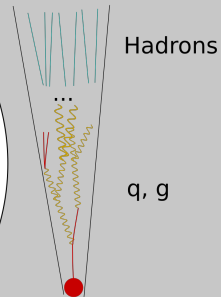


Collision sets
up geometry

IP-Glasma IC,
evolving with hydro

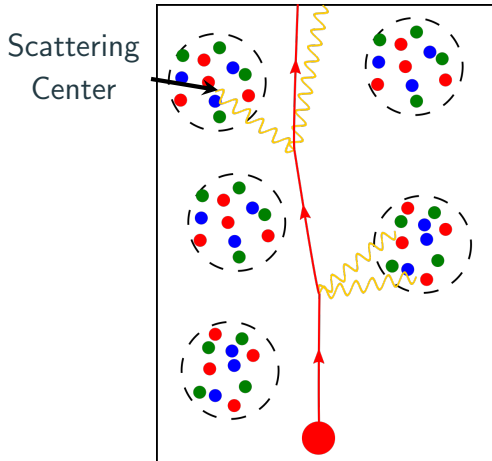


Hadronisation
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Energy loss in QGP

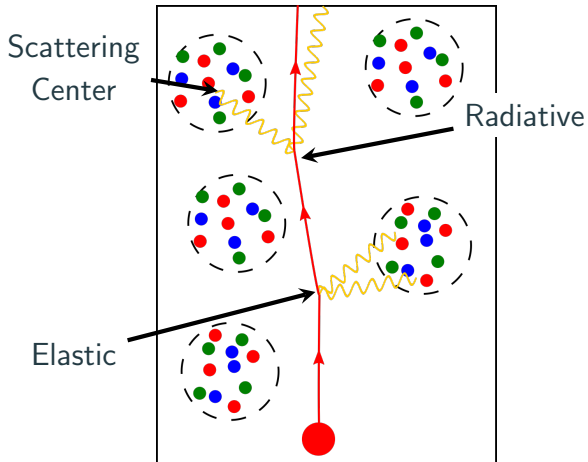
- *Radiative* (DGLV): Assume few, hard scatters and large pathlength assumption $L \gg \lambda$
- *Elastic*: Central limit theorem (large num. of scatters)
- Central $A + A$: $L \sim 5$ fm, $\lambda \sim 1$ fm
- Central $p + A$: $L \sim 1$ fm, $\lambda \sim 1$ fm



(Gyulassy et al. 2001, nucl-th/0006010, Djordjevic et al. 2004, nucl-th/0310076, Braaten et al. 1991, 10.1103/PhysRevD.44.R2625)

Energy loss in QGP

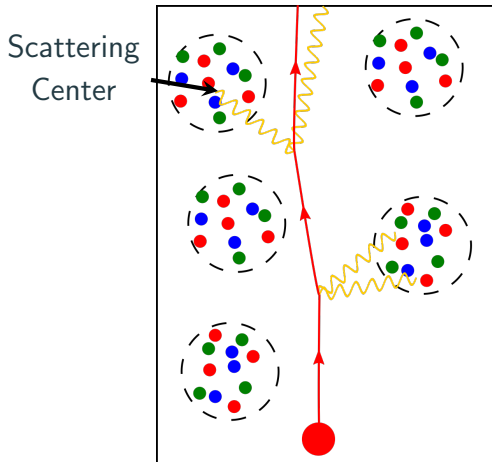
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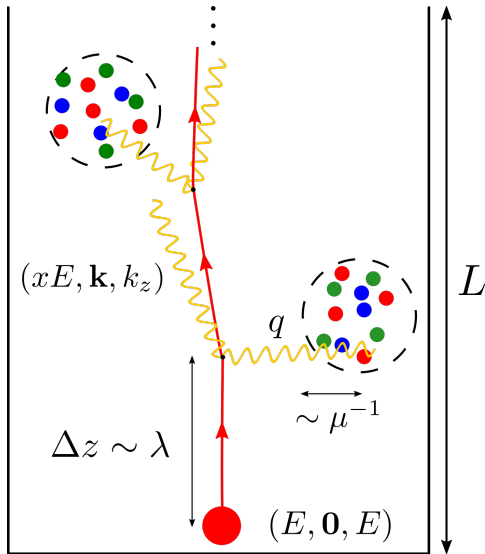
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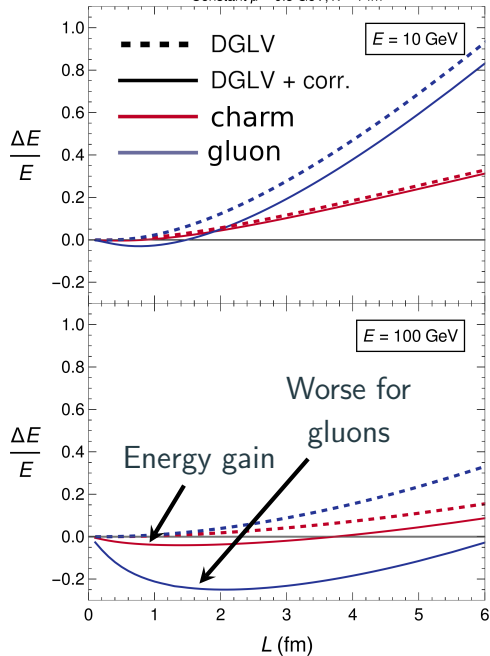
**Applicability of conventional $A + A$
techniques for $p + A$?**

Short path length corrections to radiative E-loss

Following arXiv:1511.09313 by Kolbé and Horowitz

- Weakening of assumptions:
 $1/\mu \ll \Delta z \sim \lambda \ll L$
 $\mapsto 1/\mu \ll \lambda$,
(*well separated assumption*)
- Important for small systems





Correction results in:

- Breaking of *color triviality*
- Possibility of *energy gain*
- Nontrivial correction for *all path lengths*
- Correction grows *faster in E* than uncorrected result

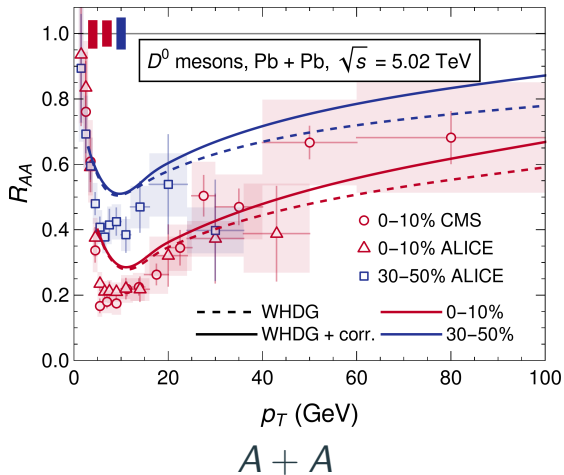
$$\begin{aligned}
\frac{dN}{dx} = & \frac{C_R \alpha_s L}{\pi \lambda_g} \int \frac{d^2 \mathbf{q}_1}{\pi} \frac{\mu^2}{(\mu^2 + \mathbf{q}_1^2)^2} \int \frac{d^2 \mathbf{k}}{\pi} \int d\Delta z \rho(\Delta z) \\
& \times \left[-\frac{2 \{1 - \cos [(\omega_1 + \tilde{\omega}_m) \Delta z]\}}{(\mathbf{k} - \mathbf{q}_1)^2 + m_g^2 + x^2 M^2} \left[\frac{(\mathbf{k} - \mathbf{q}_1) \cdot \mathbf{k}}{\mathbf{k}^2 + m_g^2 + x^2 M^2} - \frac{(\mathbf{k} - \mathbf{q}_1)^2}{(\mathbf{k} - \mathbf{q}_1)^2 + m_g^2 + x^2 M^2} \right] \right. \\
& + \frac{1}{2} e^{-\mu_1 \Delta z} \left(\left(\frac{\mathbf{k}}{\mathbf{k}^2 + m_g^2 + x^2 M^2} \right)^2 \left(1 - \frac{2C_R}{C_A} \right) \{1 - \cos [(\omega_0 + \tilde{\omega}_m) \Delta z]\} \right. \\
& \left. \left. + \frac{\mathbf{k} \cdot (\mathbf{k} - \mathbf{q}_1)}{(\mathbf{k}^2 + m_g^2 + x^2 M^2) \left((\mathbf{k} - \mathbf{q}_1)^2 + m_g^2 + x^2 M^2 \right)} \{ \cos [(\omega_0 + \tilde{\omega}_m) \Delta z] - \cos [(\omega_0 - \omega_1) \Delta z] \} \right) \right]
\end{aligned}$$

where $\omega \equiv xE^+/2$, $\omega_0 \equiv \mathbf{k}^2/2\omega$, $\omega_i \equiv (\mathbf{k} - \mathbf{q}_i)^2/2\omega$,

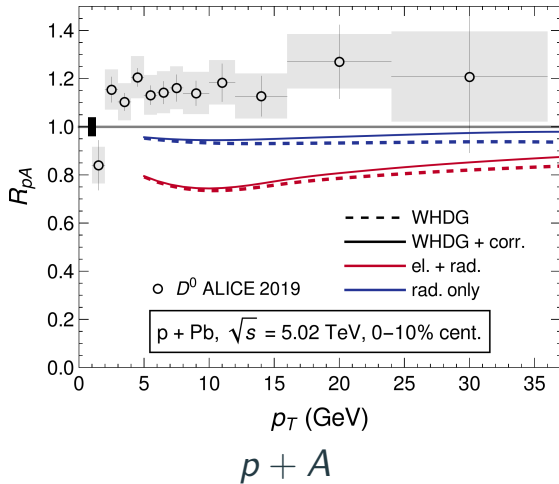
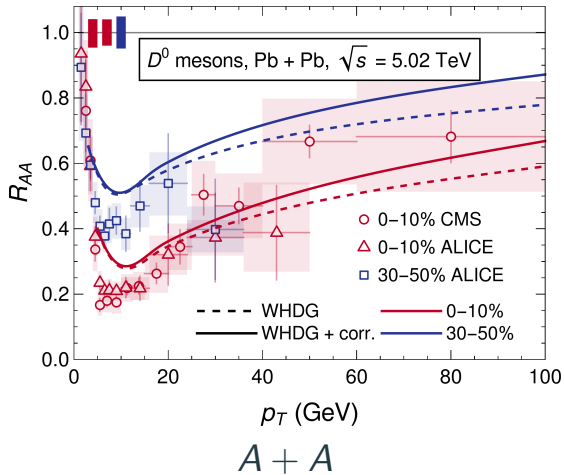
$\mu_i \equiv \sqrt{\mu^2 + \mathbf{q}_i^2}$, and $\tilde{\omega}_m \equiv (m_g^2 + M^2 x^2)/2\omega$

Predictions with the short path length correction

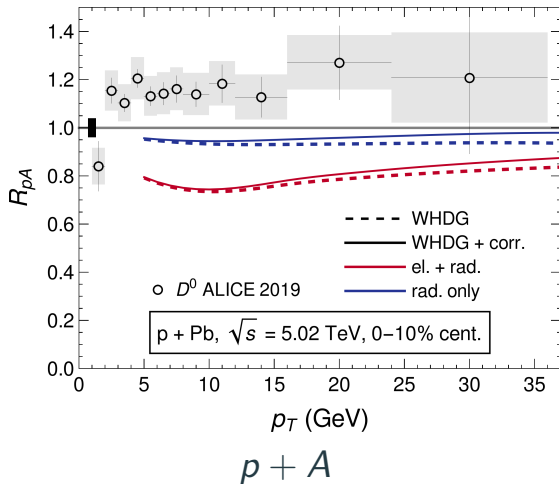
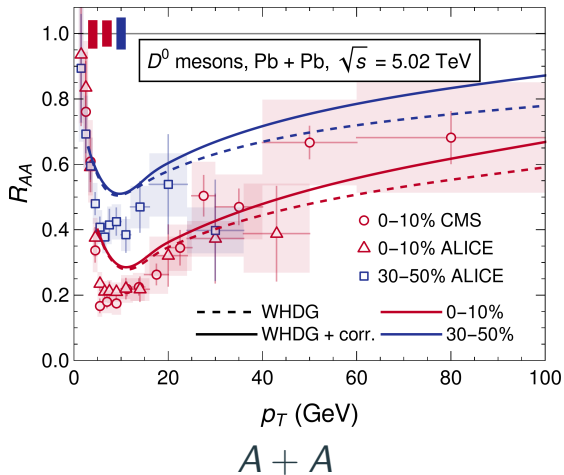
Heavy flavour predictions



Heavy flavour predictions

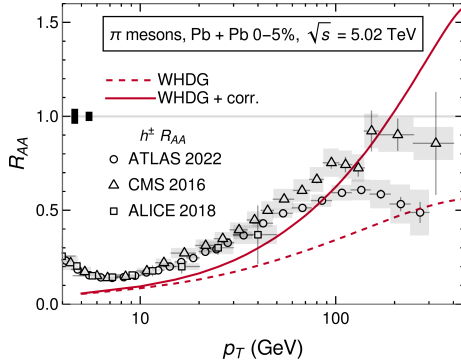


Heavy flavour predictions



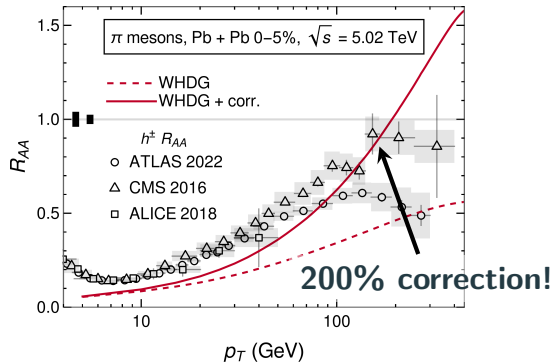
Excessive elastic E-loss in $p+A \Rightarrow$ Central limit thrm approx. *breakdown*

Light flavour predictions



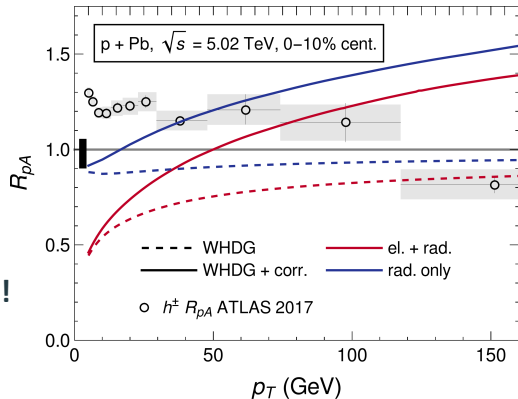
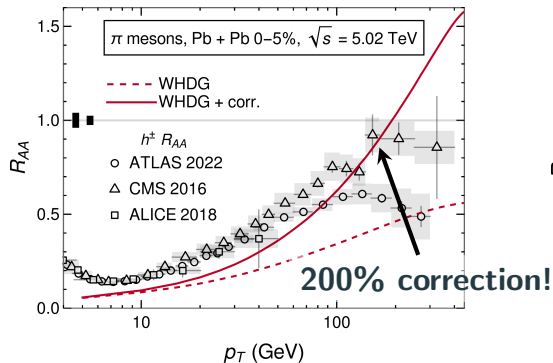
$A + A$

Light flavour predictions



$A + A$

Light flavour predictions



What's going wrong?

How physical are these results?

Breakdown of assumptions?

- Assumptions have the form $R \ll 1$ where $R = R(\mathbf{k}, \mathbf{q}, x, \Delta z)$
- Compute an *expectation value*:

$$\langle R \rangle \equiv \frac{\int d\{X_i\} R(\{X_i\}) \left| \frac{dE}{d\{X_i\}} \right|}{\int d\{X_i\} \left| \frac{dE}{d\{X_i\}} \right|},$$

and investigate whether $\langle R \rangle \ll 1$?. Note: $dE = \int dx xE dN/dx$

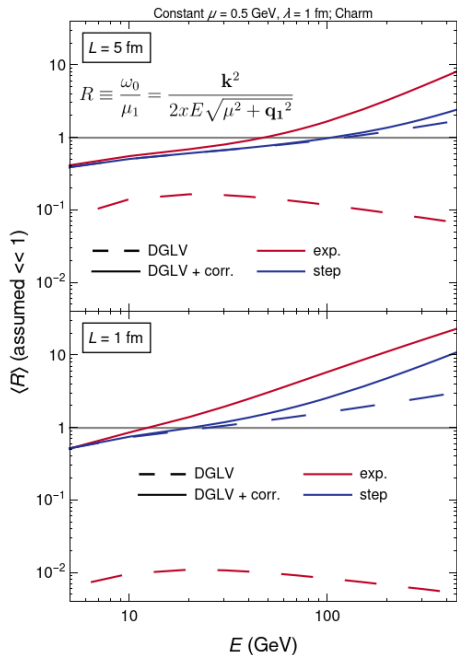
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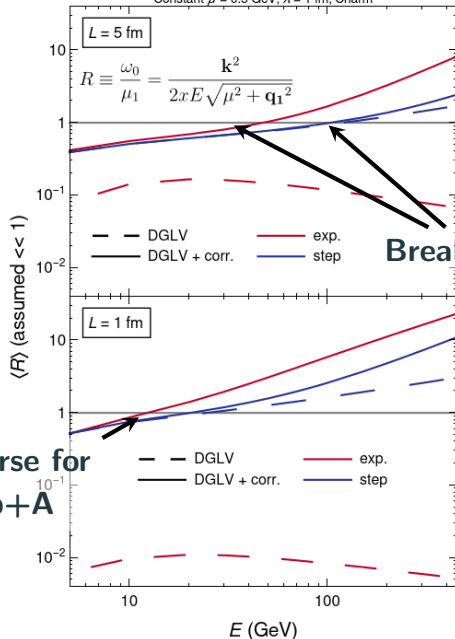
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- Also; impact of scattering center distribution? For now:
 - Exponential: $\rho_{\text{exp.}}(\Delta z) \equiv \frac{2}{L} \exp[-2\Delta z/L]$
 - Truncated step: $\rho_{\text{step}}(\Delta z) \equiv (L - \tau_0)^{-1} \Theta(\Delta z - \tau_0) \Theta(L - \Delta z)$



Plot of consistency of *large formation time* assumption:
 $\mu_1^{-1} \ll \omega_0^{-1}$.



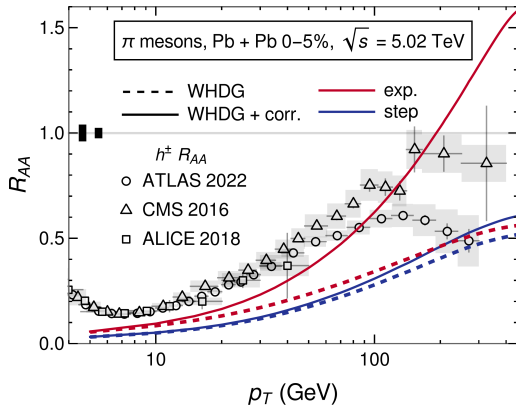
Breakdown!

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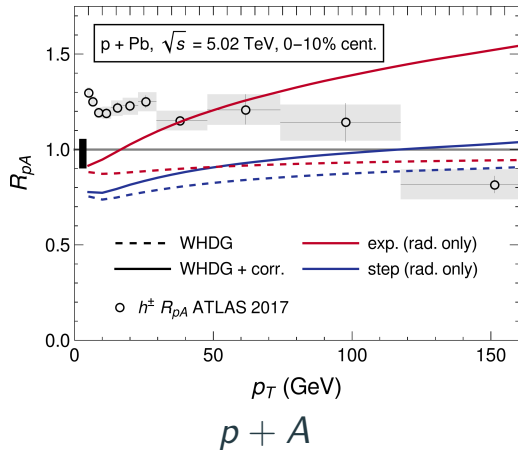
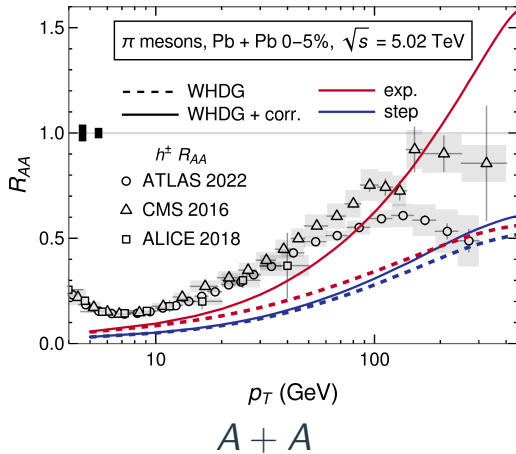
- Formation time $\tau = \omega_0^{-1} \sim \frac{2\omega}{k^2}$
- Sensitivity of breakdown to *scattering distribution*
 $\rightarrow$ impact on R_{AA} ?
- All other assumptions are satisfied self-consistently ✓

**Worse for
p+A**

Recalculate R_{AA} with truncated
step dist.



$A + A$



Size of correction dramatically *reduced*!

Conclusions / Outlook

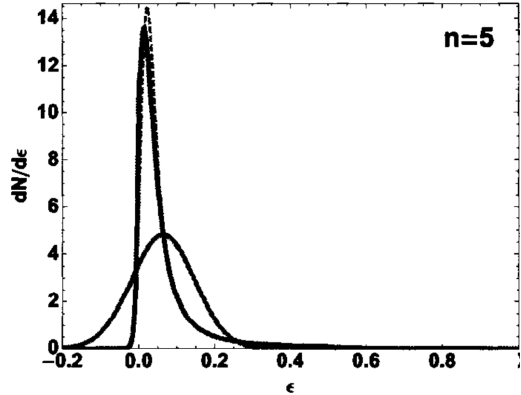
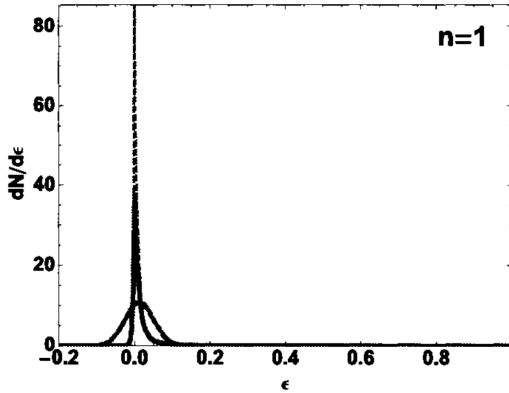
- *Elastic short pathlength corr.* needed for $p + A$
- *Short formation time corr.* to radiative E-loss
- Final state radiation (partially) responsible for *enhancement* in $p + A$?

Or just normalisation / initial state effects?

**Special thanks to my supervisor
and SA-CERN.**

Thanks for listening!

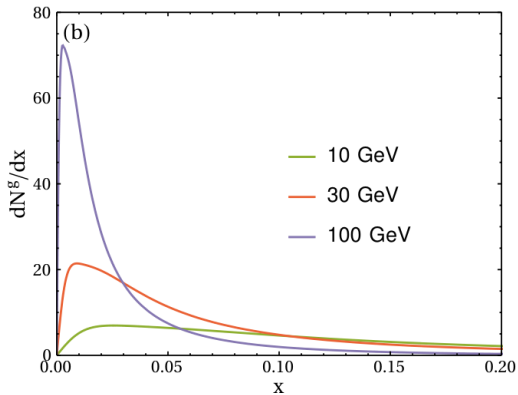
Elastic E-loss: Central limit theorem



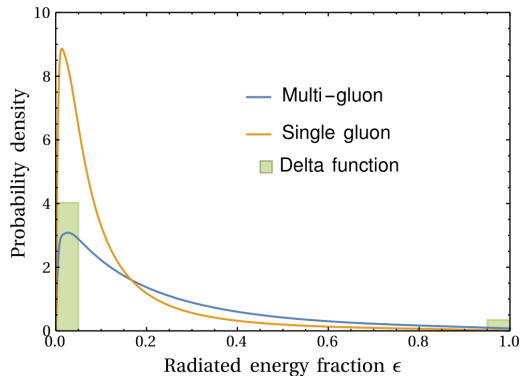
Fractional collisional elastic energy loss distribution where ϵ is the momentum fraction lost.

(Wicks 2008, PhD thesis)

Radiative emission kernel

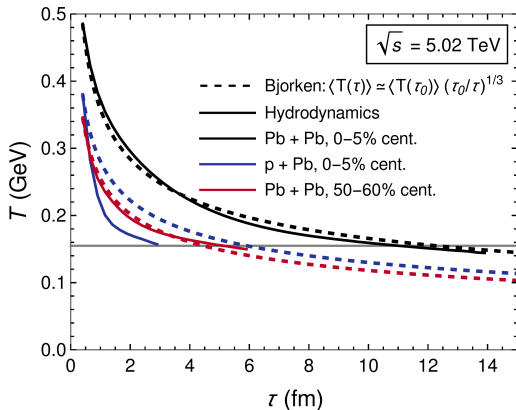


Single gluon emission kernel for Charm quarks at different energies



Single vs multiple gluon emission kernel for Charm quarks

Geometry



Temperature T of the plasma as a function of proper time τ .

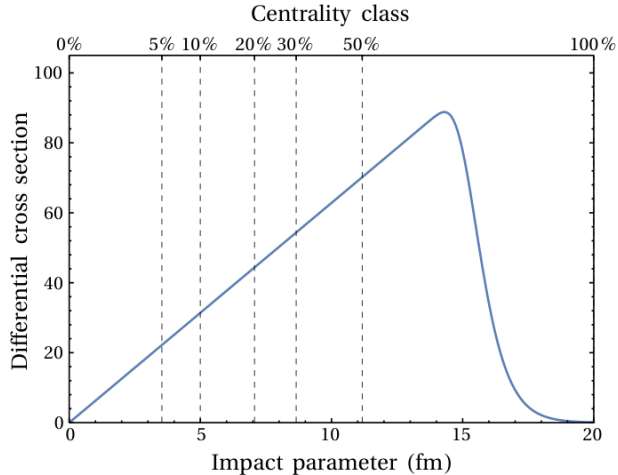
$$\langle T(\tau) \rangle \equiv \left(\frac{\int d^2x T^6(\tau, \mathbf{x})}{\int d^2x T^3(\tau, \mathbf{x})} \right)^{1/3} \quad (1)$$

where

$$\rho_{\text{part}}(\tau, \mathbf{x}) = \frac{\zeta(3)}{\pi^2} (16 + 9n_f) T^3(\tau, \mathbf{x}), \quad (2)$$

is the nucleon participant density.

Centrality explanation



Connecting centrality (experiment) and impact parameter (theory)

Making a prediction

- Interpret dN/dx as a probability
- Total probability for E-loss is the convolution $P_{\text{tot}}(\epsilon) = \int dx P_{\text{rad}}(x)P_{\text{el}}(\epsilon - x)$
- The R_{AA} is schematically

$$R_{AA} = \text{hadronization} \otimes \text{geometry} \otimes \underbrace{\int dx P_{\text{tot}}(x)(1-x)^{n(p_T)}}_{\text{E-loss in brick}}, \quad (3)$$

where $n(p_T)$ and hadronization are measured.

Accessing R_{AA} theoretically

Assume slowly-varying power law production spectrum:

$$\frac{dN_{\text{prod}}^q}{dp_i}(p_i) \propto \frac{1}{p_i^{n(p_i)}}, \quad (4)$$

leads to

$$R_{AA}^q(p_T) = \int d\epsilon P_{\text{tot}}(\epsilon, p_T) (1 - \epsilon)^{n(p_T)-1}. \quad (5)$$

Averaging over geometry:

$$\langle R_{AA}^q(p_T) \rangle_{\text{geom.}} = \int dL_{\text{eff}} \rho(L_{\text{eff}}) \times \int d\epsilon P_{\text{tot}}(\epsilon, \{p_T, L_{\text{eff}}, \langle T(\tau_0) \rangle\}) (1 - \epsilon)^{n(p_T)-1}. \quad (6)$$

Asymptotic energy loss

$$\frac{\Delta E_{\text{corr.}}}{E} = \frac{C_R \alpha_s}{2\pi} \frac{L}{\lambda_g} \left(-\frac{2C_R}{C_A} \right) \frac{\log \left(\frac{2\textcolor{red}{E}L}{2+\mu L} \right)}{2+\mu L}, \quad (7)$$

$$\frac{\Delta E_{\text{DGLV}}}{E} = \frac{C_R \alpha_s}{4} \frac{L^2 \mu^2}{\lambda_g} \frac{1}{\textcolor{red}{E}} \log \frac{\textcolor{red}{E}}{\mu}. \quad (8)$$

(Kolbé et al. 2019, 1511.09313; Gyulassy et al. 2001, nucl-th/0006010)